

1 eq1:=Dv=Vv\*t-1/2\*g\*t^2 // Dv - vert position; Vv - initial vert velocity

$$Dv = (Vv \cdot t - \frac{g \cdot t^2}{2}) \quad (1)$$

2 eq1a:=subst(eq1,Vv=Vb) // 45 deg launch angle

$$Dv = (Vb \cdot t - \frac{g \cdot t^2}{2}) \quad (2)$$

3 eq2:=lhs(eq1a)=factor(rhs(eq1a))

$$Dv = (\frac{t(2 \cdot Vb - t \cdot g)}{2}) \quad (3)$$

4 eq3:=t=subst(solve(eq1a,t),Dv=0)[0]

$$t = (\frac{Vb + Vb}{g}) \quad (4)$$

5 assume(Vb>0)

$$Vb \quad (5)$$

6 eq4:=simplify(eq3) // time in the air

$$t = (\frac{2 \cdot Vb}{g}) \quad (6)$$

7 eq5:=Dh=Vh\*t // Dh - horiz distance traveled

$$Dh = (Vh \cdot t) \quad (7)$$

8 eq5a:=subst(eq5,Vh=Vb) // 45 deg launch angle

$$Dh = (Vb \cdot t) \quad (8)$$

9 eq6:=subst(eq5a,eq4)

$$Dh = (\frac{Vb \cdot 2 \cdot Vb}{g}) \quad (9)$$

$$\boxed{10} \text{ eq7:=Vb=solve(eq6,Vb)[0]}$$

$$Vb = \left( \frac{\sqrt{2}\sqrt{Dh \cdot g}}{2} \right) \quad (10)$$

$$\boxed{11} \text{ vars01:=tran([Dh=25_ft,g=_g_]) // convert(_g_(ft*s^-2))}$$

$$\left( \begin{array}{l} Dh = (25\_ft) \\ g = (1\_g-) \end{array} \right) \quad (11)$$

$$\boxed{12} \text{ eq8:=subst(eq7,vars01)}$$

$$Vb = \left( \frac{\sqrt{2}\sqrt{(25\_ft \cdot \_g-)}}{2} \right) \quad (12)$$

$$\boxed{13} \text{ eq8a:=lhs(eq8)=convert(usimplify(rhs(eq8))_(ft*s^-1))}$$

$$Vb = \left( 20.0543164171 \frac{ft}{s} \right) \quad (13)$$

$$\boxed{14} \text{ eq9:=Vl=Vb*sqrt(2)}$$

$$Vl = (Vb\sqrt{2}) \quad (14)$$

$$\boxed{15} \text{ eq10:=subst(eq9,eq8a)}$$

$$Vl = \left( 28.3610862611 \frac{ft}{s} \right) \quad (15)$$

$$\boxed{16} \text{ eq11:=Dl=1/2*A1*tl^2 // Dl - launcher travel; A1 - launch acceleration; tl = time to launch}$$

$$Dl = \left( \frac{A1 \cdot tl^2}{2} \right) \quad (16)$$

$$\boxed{17} \text{ eq12:=Vl=A1*tl}$$

$$Vl = (A1 \cdot tl) \quad (17)$$

$$\boxed{18} \text{ eq13:=tl=solve(eq12,tl)[0]}$$

$$tl = \left( \frac{Vl}{A1} \right) \quad (18)$$

$$\boxed{19} \text{ eq14:=simplify(subst(eq11,eq13))}$$

$$Dl = \left( \frac{Vl^2}{2 \cdot Al} \right) \quad (19)$$

$$\boxed{20} \text{ eq15:=Al=solve(eq14,Al)[0]}$$

$$Al = \left( \frac{Vl^2}{2 \cdot Dl} \right) \quad (20)$$

$$\boxed{21} \text{ eq16:=Dl=2*pi*Rl*angl/360 // Rl - radius launch arm; angl - launch arm sweep angle}$$

$$Dl = \left( \frac{2 \cdot \pi \cdot Rl \cdot angl}{360} \right) \quad (21)$$

$$\boxed{22} \text{ vars02:=tran([ Rl=1_ft, angl=45])}$$

$$\left( \begin{array}{l} Rl = (1\_ft) \\ angl = 45 \end{array} \right) \quad (22)$$

$$\boxed{23} \text{ eq17:=subst(eq16,vars02)}$$

$$Dl = (0.785398163397\_ft) \quad (23)$$

$$\boxed{24} \text{ eq18:=eval(subst(eq15,[eq10,eq17]))}$$

$$Al = \left( 512.065886703 \frac{\_ft^2 \cdot \_ft^{-1.0}}{\_s^2} \right) \quad (24)$$

$$\boxed{25} \text{ eq18a:=lhs(eq18)=convert(usimplify(rhs(eq18))\_ft*s^{-2})}$$

$$Al = \left( 512.065886703 \frac{\_ft}{\_s^2} \right) \quad (25)$$

$$\boxed{26} \text{ eq19:=Fl=Mp*Al // Fl - launch average force; Mp - payload mass}$$

$$Fl = (Mp \cdot Al) \quad (26)$$

$$\boxed{27} \text{ eq20:=subst(eq19,[ Mp=1\_lb, eq18a ])}$$

$$Fl = \left( 512.065886703 \frac{\_ft \cdot \_lb}{\_s^2} \right) \quad (27)$$

28 `eq21:=lhs(eq20)=convert(rhs(eq20),lb)`

$$F_l = (15.9119171679 \text{ lb}) \tag{28}$$

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